

# Time-Resolved Analysis of High-Power-Laser Produced Plasma Expansion in Vacuum

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**Abstract.** Here we consider the results of an experimental investigation of the temporal evolution of plasmas produced by high power laser irradiation of various types of target materials. The experiment was performed at the LULI Laboratory (Ecole Polytechnique, Paris). We have developed a method to analyze time-resolved streak-camera images and analyzed a number of results obtained with various materials.

## INTRODUCTION

The aim of this work is to analyze the process of plasma generation and expansion by high power laser irradiation of different materials, in order to find the temporal-spatial distribution of electron plasma density, to find the temporal and spatial profiles of characteristic velocities of plasma expansion and to analyze these behaviors vs. the atomic number  $Z$  and/or the laser energy.

The investigation of hydrodynamics expansion of laser-produced plasmas (in the intensity range  $I \approx 10^{14}$  W/cm<sup>2</sup>) is of fundamental importance for several physics areas such as inertial confinement fusion. Although several theoretical models of plasma expansion were developed already in the 70's and in the 80's [1-3] and many experiments have studied this aspect, still there are not many "clean" experimental results. Indeed most experiments are influenced by 2D effects in the hydro expansion of the plasma, which arise as a consequence of the small focal spots, which were needed to produce the relatively high laser intensity of interest in these experiments.

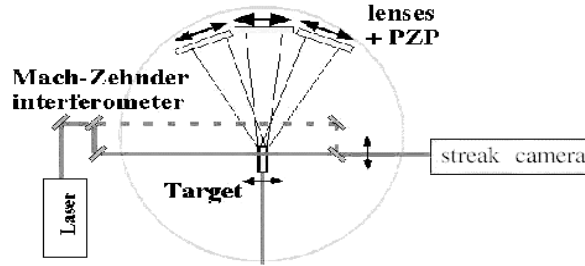
In recent years, several techniques have been introduced which allow the production of "flat-top" intensity profiles. Hence one fundamental experimental parameter, the laser intensity on target, is clearly defined, which is not the case with the usual Gaussian-like intensity distribution or, even worse, with focal spots affected by laser hot spots. This allows a well-characterized parametric study of plasma expansion. Also, 2D effects in plasma expansion are strongly reduced, producing a situation much closer to that described by 1D theoretical models. One of such technique is that of Phase Zone Plates (PZP [4]) which appeared in recent years, as an useful investigation tool, and which was also used in our experiment.

## EXPERIMENTAL SET UP

The experimental set up includes a Nd:glass high power laser system with typical intensity of  $10^{14}$  W/cm<sup>2</sup> and duration 600 ps, a probe beam (Nd:YAG converted to 2 $\omega$ ) coupled to an interferometer and to a streak-camera with

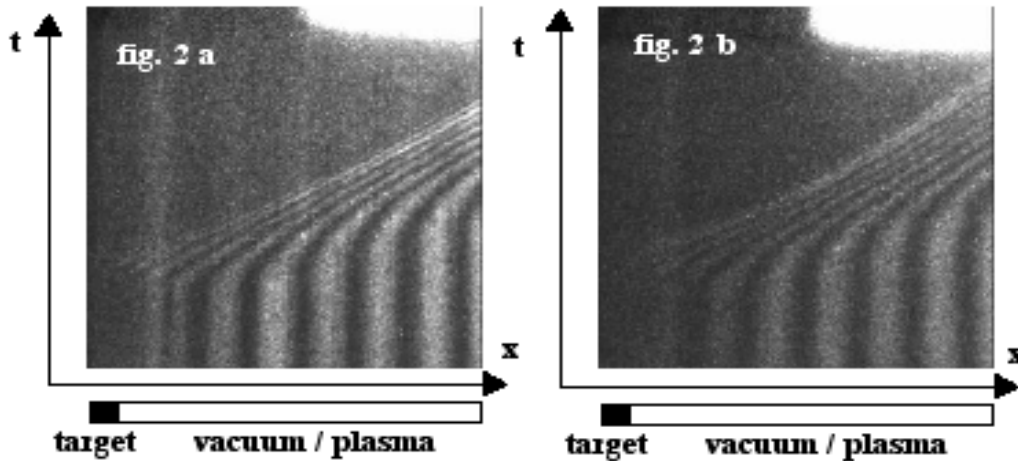
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ps resolution. The diagnostic system allows the evolution of the plasma density profile to be measured as a function of time. Different targets (CH, Al, Au) have been in the experiment, with different radiative properties. In particular plasma expansion with Au targets should be strongly influenced by radiation (XUV) transport [5], while, in the case of CH targets, energy transport should be determined by electrons only. Such phenomena are a key problem in the physics of Inertial Confinement Fusion (ICF) driven by lasers.



**FIGURE 1.** Typical experimental set-up used at LULI

Phase Zone Plates (PZP) were used to smooth the laser beam (remove large-scale hot spots) and produce a flat-top irradiation profile, reducing 2D in plasma expansion [4]. The experimental set-up is shown in fig. 1. Fig. 2 shows typical experimental streak-camera images: a) CH and b) Al targets accordingly. The total image dimensions are 375  $\mu\text{m}$  (horizontal scale) and (1.065 ns vertical scale).



**FIGURE 2.** Typical interferograms recorded with the streak camera: a) CH and b) Al targets. The total image dimensions are 375  $\mu\text{m}$  (horizontal scale) and (1.065 ns vertical scale).

## DETERMINATION OF PLASMA DENSITY

Here we introduce the method used for the analysis of interferometric images, like those presented in fig. 2. The phase shift in a point  $x$  of the interferometric picture from classical optics is  $\Delta\Phi_d(x) = 2\pi\alpha x / \lambda$ , where  $\alpha$  is the angle

between the probe and reference beams the in interferometer; and  $\lambda$  the wavelength of the laser beam. The plasma-induced phase shift is  $\Delta\phi_{plasma}(x, t) = \frac{2\pi d}{\lambda} \left( 1 - \sqrt{1 - \frac{N_e(x, t)}{n_c}} \right)$ , where  $N_e$  is the density of free electrons,

$n_c = \frac{4\pi^2 c^2 \epsilon_0 m_e}{\lambda^2 e^2}$ , the critical density,  $\lambda$  the laser wavelength. Here  $d$  is the transversal dimension of the plasma

(along probe beam, i.e. perpendicularly to  $x$ ). In this preliminary analysis, we have taken  $d = 400 \mu\text{m}$ , corresponding to the FWHM of the laser focal spot created by the PZPs. Therefore the density can be obtained from the phase shift

as:  $N_e = n_c \left( 1 - \left( 1 - \frac{\Delta\phi_{plasma} \lambda}{2\pi d} \right)^2 \right)$ . In the limiting case  $N_e \ll n_c$ , we get  $N_e \approx \Delta N_e i$ , where  $\Delta N_e = n_c \lambda / d$ , and where

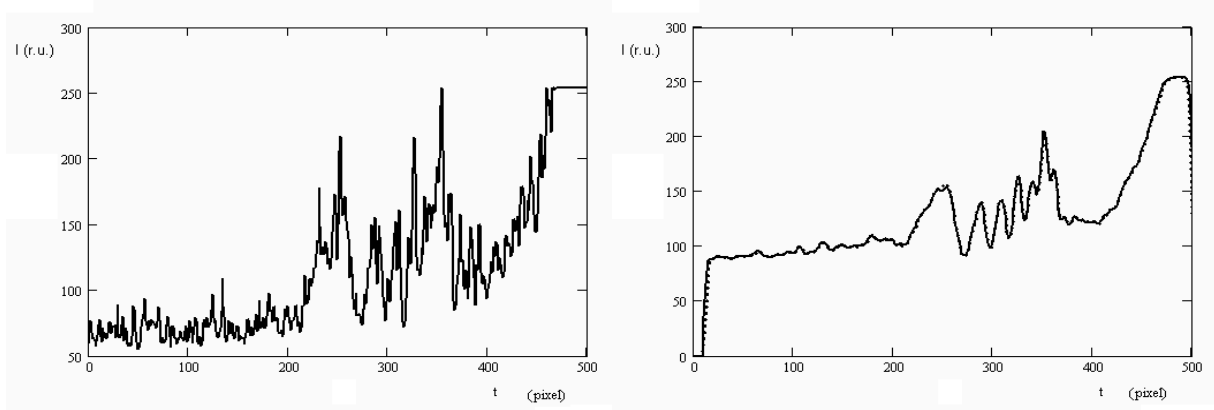
$i$  is the number of  $\pi$ -phase shifts. Hence, every phase shift of  $\pi$  along the temporal axis corresponds to a density

jump  $\Delta N_e = n_c \left( \left( 1 - \frac{\Delta\phi_{plasma} \lambda}{2\pi d} \right)^2 - \left( 1 - \frac{(\Delta\phi_{plasma0} + \pi) \lambda}{2\pi d} \right)^2 \right)$  in the general case, or  $\Delta N_e = n_c \lambda / d$ , in the case

$N_e \ll n_c$ .

In the following step of the analysis, we consider the points on the  $x$ -axis (spatial dimension), which initially, i.e. before plasma production, correspond to maxima and minima of the interferograms, and we follow here the time evolution of the density  $N_e$  in steps of  $\Delta N_e$ .

For the analysis of the interferograms we have applied a technique of averaging with time shifts, which is similar to the application of the direct Radon transformation, which was discussed in [6].



**FIGURE 3 (a)**, time-dependence of intensity in the streak-camera image in fig. 2a, for  $x_0=481$  pixels; **(b)**, time-dependence of intensity in the streak-camera image in fig. 2a, for  $x_0=481$  after time-shift averaging in the spatial interval  $\pm 20$  pixel. The dotted line corresponds to characteristic velocity 1.6, the solid line to 1.8. Finally a Gauss-filter by  $t$  as been applied

## ANALYSIS OF INTERFEROMETRICAL IMAGES

For the analysis of experimental interferograms, we have attempted to consider a precise numerical method based on averaging with shift on the time axis.

Indeed, if consider one interferogram, as in fig. 2, and we plot the intensity corresponding to one given position  $x_0$  (vertical densitometry), the presence of a very strong noise (fig. 3 (a)) can result either in neglecting or shifting of real extremes of phase shift, or in the appearance of false extremes. But on the other hand, averaging of several of such densitometries on a small interval  $\Delta x_0$ , centred around  $x_0$ , does not give good results, because it smoothes the picture.

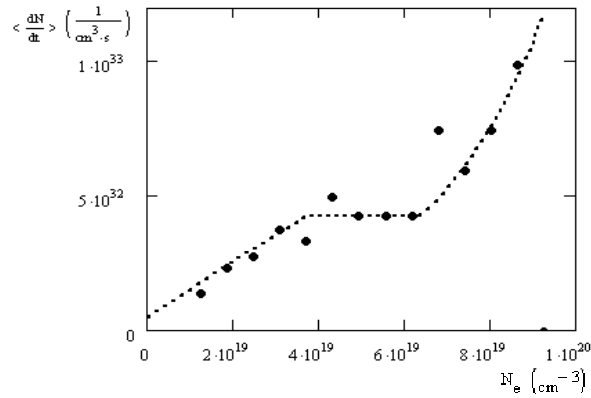
In alternative, the averaging with time shifts, with a characteristic velocity more or less correspondent to real velocity, gives a good resolution and a good contrast in the obtained densitometry.

Fig. 3 (a) and (b) give the illustration of the method for the precise determination of extremes in the interferometric streak-camera image, shown in the fig. 2 (a), where  $x_0=481$  pixels, corresponding to the first minimum from the right. The horizontal time scale is also in pixels. The real scale is 512 / 512 pixels for 375  $\mu\text{m}$  / 1065 ps. The vertical scale, giving the intensity on the streak-camera image, is in arbitrary units. How we can see from fig. 3 (b), the differences between locations of extremes for a quite wide range of characteristic time-shift velocities are not more than 1 pixel (the principle limit), showing that our results are quite reliable.

## RESULTS AND DISCUSSION

Let us turn back to fig. 2. For the each fixed  $x$ , we find 3 zones: (i) the first, where the signal is only modulated in  $x$  and independent from  $t$  (vertical interference fringes), (ii) the second one, where the signal significantly depends on  $t$  (inclined interference fringes), and (iii) third one, practically uniform where the interference fringes disappear. The first, up to a time  $t_0(x)$ , correspond to the situation without any plasma. At the time  $t_0$ , the first plasma reaches the point  $x$  (or at least a plasma with a density sufficient to produce a measurable phase shift). The second zone ends at the time  $t_{cr}$ , at which the plasma density overcomes some critical value, so that the probe beam is refracted away from the collecting optics. After  $t_{cr}$ , of course the fringes disappear and it becomes impossible to determine the plasma density. So, the zone which we can investigate is limited by the curves  $t_0(x)$  and  $t_{cr}(x)$ , which separate the region of non-zero and non-overcome electron density.

Within this zone, for each fixed  $x$ , we can further distinguish 3 regions: (i) first growth, (ii) constant behaviour, and (iii) final fast growth. For a better analysis of such behaviour, we consider the dependence of the growth velocity  $dN_e/dt$  from  $N_e$  (fig. 4 shows such dependence for  $x=303 \mu\text{m}$ ).



**FIGURE 4.** Velocity growth of electron density, vs. electron density, for  $x=303 \mu\text{m}$ , as deduced from fig. 1 a.

Starting from the typical dependence shown in fig. 4, we can write:

$$dN_e/dt = (\Delta N_e / \Delta t_{||}) f(N_e, x) \quad (1)$$

where  $\Delta N_e$  and  $\Delta t_{||}$  corresponds to the previously introduced density jump inducing a  $\pi$ -phase shift and to the time difference between value of  $N_e$  with phase shift  $\pi$  in the interferometric picture in the second (constant) region. Solving this differential equation we can find the formula for the time  $t(N_e, x)$ , at which an electron density  $N_e$  is

realized in the point  $x$ . This is  $t(N_e, x) = t_0(x) + \frac{\Delta t_{\parallel}}{\Delta N_e} \int_0^{N_e} \frac{dN_e}{f(N_e, x)}$  where  $t_0(x)$  is the time, where the first plasma reaches the point  $x$ , as before. For the function  $f(N_e, x)$  we could find an empirical equation:

$$f(N_e, x) = \begin{cases} A(x) + (1 - A(x)) \cdot (N_e / N_{cr1}) & , \quad N_e < N_{cr1} \\ 1 & , \quad N_{cr1} < N_e < N_{cr2}(x) \\ \exp(B(x) \cdot ((N_e / N_{cr2}(x)) - 1)) & , \quad N_e > N_{cr2}(x) \end{cases} \quad (2)$$

where  $A(x)$  is an empirical linear function characterizing of the growth of  $N_e$  in the first region;  $B(x) = \ln(1/A(x))$ , and  $N_{cr1}$  and  $N_{cr2}$  are the electron densities corresponding to the beginning and the end of the constant phase in fig. 4. It is necessary to remark that if formally  $N_{cr1} > N_{cr2}$  the function  $f(x)$  has no constant region. We can finally find the dependence of  $N_e$  from  $t$  and  $x$ . If the function  $f(x)$  has a constant region, this is:

$$N_e(t, x) = \begin{cases} \frac{N_{cr1} \cdot A(x)}{1 - A(x)} \cdot \left( \exp\left(\frac{(t - t_0(x)) \cdot (1 - A(x)) \cdot \Delta N_e}{N_{cr1} \cdot \Delta t_{\parallel}}\right) - 1 \right) & , \quad t < t_{cr1}(x) \\ N_{cr1} + (\Delta N_e / \Delta t_{\parallel}) \cdot (t - t_{cr1}(x)) & , \quad t_{cr1}(x) < t < t_{cr2}(x) \\ N_{cr2}(x) \cdot \left( B(x) - \ln\left(\exp(B(x) - 1) - \frac{(t - t_{cr2}(x)) \cdot N_{cr2}(x)}{\Delta t_{\parallel} \cdot \Delta N_e}\right) \right) & , \quad t_{cr2}(x) < t \end{cases} \quad (3)$$

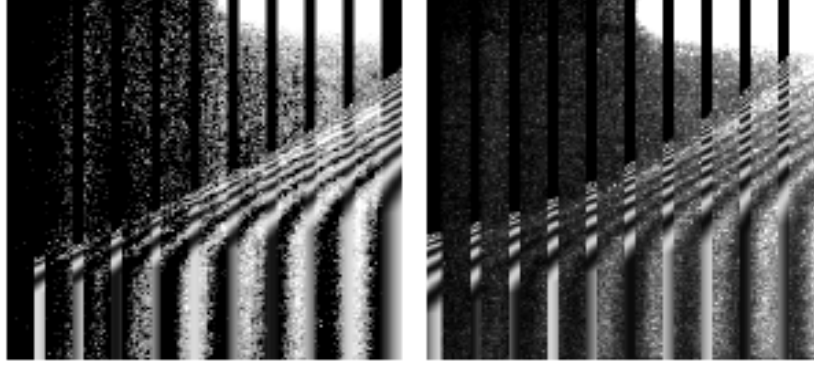
$$\text{where } t_{cr1}(x) = t_0(x) + \frac{\Delta t_{\parallel} N_{cr1} B(x)}{\Delta N_e \cdot (1 - A(x))} \quad t_{cr2}(x) = t_{cr1}(x) + \Delta t_{\parallel} \cdot \frac{N_{cr2}(x) - N_{cr1}}{\Delta N_e}$$

while, if the function  $f(x)$  has no constant region

$$N_e(t, x) = \begin{cases} \frac{N_{cr1} \cdot A(x)}{1 - A(x)} \cdot \left( \exp\left(\frac{(t - t_0(x)) \cdot (1 - A(x)) \cdot \Delta N_e}{N_{cr1} \cdot \Delta t_{\parallel}}\right) - 1 \right) & , \quad t < t_{cr2}(x) \\ N_{cr2}(x) \cdot \left( B(x) - \ln\left(\exp(B(x) - 1) - \frac{(t - t_{cr2}(x)) \cdot N_{cr2}(x)}{\Delta t_{\parallel} \cdot \Delta N_e}\right) \right) & , \quad t_{cr2}(x) < t \end{cases} \quad (4)$$

where  $t_{cr2}(x) = t_0(x) + \Delta t_{\parallel} \cdot \frac{N_{cr1}(x)}{1 - A(x)} \cdot \ln\left(1 + \frac{N_{cr2}(x) \cdot (1 - A(x))}{A(x) \cdot N_{cr1}(x)}\right)$ . From our preliminary analysis, we can conclude that  $N_{cr1}$  is more or less independent on  $x$ ,  $N_{cr2}$  strongly depends on the point  $x$ ,  $\Delta t_{\parallel}$  is practically independent from  $x$  for the CH target.

From the calculated values of  $N_e(t, x)$  we can reconstruct the interferograms. We can observe (see fig. 5, which presents the comparison between reconstructed interferograms (stripes without noise) and experimental ones (stripes with noise) for the cases presented in fig. 1, CH (left) and Al (right) targets.) how these correspond very well to the experimental interferograms for *all* values of  $x$  and  $t$ .



**FIGURE 5.** Comparison between reconstructed interferograms (stripes without noise) and experimental ones for the cases presented in fig. 1, CH (left) and Al (right) targets.

## CONCLUSION

In conclusion, we have found a reasonable way to analyze the interferograms and reconstruct them, and we have found some phenomenological behavior. It should be stressed that the values of  $N_e$ , which we calculated, are **NOT** the real values of electron density. Indeed they have been calculated by assuming a plasma transversal size  $d = 400 \mu\text{m}$  (equal to the FWHM size of the focal spot) and keeping it constant in time. Hence in reality the variation evidenced in fig. 4 rather corresponds to the evolution of the line integral  $\int N_e(x, y, t) dy$  ( $y$  being the coordinate along the probe beam, perpendicular to  $x$ ) which we assumed to be  $\approx (N_e d)$ . A more proper analysis will need to consider the time evolution of the plasma transversal size, through a 2D hydrodynamics modeling.

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